

Lecture 4: Convolutional Neural Networks

Deep Learning @ UvA

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- What are the Convolutional Neural Networks?
- Differences from standard Neural Networks
- Why are they important in Computer Vision?
- How to train a Convolutional Neural Network?

Convolutional Neural Networks



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Depth

Height

Width

1920x1080x3 = 6,220,800 input variables

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CONVOLUTIONAL NEURAL NETWORKS - 7

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Image has shifted a bit to the up and the left!

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CONVOLUTIONAL NEURAL NETWORKS - 10

- An image has spatial structure
- Huge dimensionality
 - A 256x256 RGB image amounts to ~200K input variables
 - 1-layered NN with 1,000 neurons \rightarrow 200 million parameters
- \circ Images are stationary signals \rightarrow they share features
 - After variances images are still meaningful
 - $^{\circ}$ Small visual changes (often invisible to naked eye) ightarrow big changes to input vector
 - Still, semantics remain
 - Basic natural image statistics are the same

Input dimensions are correlated

Traditional task: Predict my salary!

	Level of education	Age	Years of experience	Previous job	Nationality_
Shift 1 dimension <	"Higher"	28	6	Researcher	Spain
	Level of education	Age	Years of experience	Previous job	Nationality
	Spain	"Higher"	28	6	Researcher

Vision task: Predict the picture!



First 5x5 values

array([[51, 49, 51, 56, 55], [53, 53, 57, 61, 62], [67, 68, 71, 74, 75], [76, 77, 79, 82, 80], [71, 73, 76, 75, 75]], dtype=uint8)



First 5x5 values

array([[58, 57, 57, 59, 59], [58, 57, 57, 58, 59], [59, 58, 58, 58, 58], [61, 61, 60, 60, 59], [64, 63, 62, 61, 60]], dtype=uint8)

Convolutional Neural Networks

• Preserve spatial structure by convolutional filters

• Tackle huge input dimensionalities by local connectivity and parameter sharing

• Robust to local variances by spatial pooling

Preserving spatial structure

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- o Images are 2-D
 - 3-D if you also count the extra channels
 - RGB, hyperspectral, etc.

What does a 2-D input really mean?
Neighboring variables are locally correlated





Example filter when K=1

e.g. Sobel 2-D filter





Learnable filters

- Image processing and Computer Vision has many handcrafted filters
 - Canny, Sobel, Gaussian blur, smoothing, lowlevel segmentation, morphological filters, Gabor filters
- Are they optimal for recognition?
- Can we learn optimal filters from our data instead?
- Are they going resemble the handcrafted filters?



W ₁₁	<i>W</i> ₁₂	W ₁₃
<i>w</i> ₂₁	<i>W</i> ₂₂	<i>W</i> ₂₃
W_{31}	W ₃₂	<i>W</i> ₃₃

2-D Filters (Parameters)

• If images are 2-D, parameters should also be organized in 2-D

- That way they can learn the local correlations between input variables
- That way they can "exploit" the spatial nature of images

Grayscale



3-D Filters (Parameters)

• Similarly, if images have k channels, parameters should also have k channels



What does a 3-D filter look like?

2-D filter







Hypothesis

- Image statistics are not location dependent
 Natural images are stationary
- The same filters should work on every corner of the image similarly
- Perhaps move and reuse the same (red, yellow, green) filter across the whole image?







Oríginal ímage





Convolutional filter 1







Convolutional filter 1

1	0	1
0	1	0
1	0	1





Output dimensions after convolution



Definition The convolution of two functions f and g is denoted by * as the integral of the product of the two functions after one is reversed and shifted $(f * g)(t) \stackrel{\text{def}}{=} \int_{-\infty}^{\infty} f(\tau)g(t-\tau) d\tau = \int_{-\infty}^{\infty} f(t-\tau)g(\tau) d\tau$



• Activation function

$$a_{rc} = \sum_{i=-a}^{a} \sum_{j=-b}^{b} x_{r-i,c-j} \cdot w_{ij}$$

• Essentially a dot product, similar to linear layer $a_{rc} \sim x_{re,gion}^T \cdot w$

• Gradient w.r.t. the parameters

$$\frac{\partial a_{rc}}{\partial w_{ij}} = x_{r-i,c-j}$$
$$\frac{\partial \mathcal{L}}{\partial w_{ij}} = \sum_{r} \sum_{c} \frac{\partial \mathcal{L}}{\partial a_{rc}} x_{r-i,c-j}$$

Local connectivity: weight connections are surface-wise local!
 The blue filter weights connect only to local orange pixels along the surface /

The weights connections are depth-wise global
 The blue filter weights connect to all orange channels across the depth

- For standard neurons, no local connectivity
 - Everything is connected to everything
 - No notion of surface or depth
 - We might as well shuffle the pixels, there is no difference



Local connectivity ≠ Convolutional filters

• Local but *non-shareable* filters are possible

• Still useful for some applications



Filters with different values depending on image location and channel ID





Assume the image is 30x30x3. 1 filter every pixel (stride =1) How many parameters in total?

24 filters along the x axis24 filters along the y axisDepth of 5

 \times 7 * 7 * 3 parameters per filter

423K parameters in total

Convolutions reduce dimensionality

- Our images get smaller and smaller
- \circ We run out of "latent pixels" \rightarrow not too deep architectures
- \circ Details are lost \rightarrow recognition accuracy drops



Zero-padding to maintain input dimensionality

*

• For s = 1, surround the image with $(h_f - 1)/2$ and $(w_f - 1)/2$ layers of 0



001011111



- Resize the image to have a size in the power of 2
- Stride s = 1
- A filter of $(h_f, w_f) = [3 \times 3]$ works quite alright with deep architectures
- Add 1 layer of zero padding

Good practices

- In general avoid combinations of hyper-parameters that do not click
 - E.g. *s* = 2
 - $[h_f \times w_f] = [3 \times 3]$ and
 - image size $[h_{in} \times w_{in}] = [6 \times 6]$
 - $\circ [h_{out} \times w_{out}] = [2.5 \times 2.5]$
 - Programmatically worse, and worse accuracy because borders are ignored

1	1	1	0	0	1
0	1	1	1	0	0
0	0	1	1	1	0
0	0	1	1	0	0
0	1	1	0	0	0

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- Aggregate multiple values into a single value
 - Invariance to small transformations
 - Reduces the size of the layer output/input to next layer \rightarrow Faster computations
 - Keeps most important information for the next layer

• Max pooling
•
$$\frac{\partial a_{rc}}{\partial x_{ij}} = \begin{cases} 1, & if \ i = i_{max}, j = j_{max} \\ 0, & otherwise \end{cases}$$

• Average pooling $\circ \frac{\partial a_{rc}}{\partial x_{ij}} = \frac{1}{r \cdot c}$



2

2.5

ConvNet Case Study I: Alexnet

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Figure 2: An illustration of the architecture of our CNN, explicitly showing the delineation of responsibilities between the two GPUs. One GPU runs the layer-parts at the top of the figure while the other runs the layer-parts at the bottom. The GPUs communicate only at certain layers. The network's input is 150,528-dimensional, and the number of neurons in the network's remaining layers is given by 253,440–186,624–64,896–64,896–43,264–4096–4096–1000.

Architectural details

18.2% error in Imagenet



Removing layer 7

1.1% drop in performance, 16 million less parameters



Removing layer 6, 7

5.7% drop in performance, 50 million less parameters



Removing layer 3, 4

3.0% drop in performance, <u>1 million</u> less parameters. <u>Why</u>?



Removing layer 3, 4, 6, 7

33.5% drop in performance. Conclusion? <u>Depth!</u>



Translation invariance



Credit: R. Fergus slides in Deep Learning Summer School 2016

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Is AlexNet translation invariant?

- o Yes
- o No
- o In some cases

Is AlexNet translation invariant?

o Yes

o No

o In some cases



Credit: R. Fergus slides in Deep Learning Summer School 2016

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Scale invariance



Credit: R. Fergus slídes in Deep Learning Summer School 2016

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Is AlexNet scale invariant?

- o Yes
- o No
- o In some cases

Is AlexNet scale invariant?

- o Yes
- o No
- \circ In some cases

Scale invariance



Credit: R. Fergus slides in Deep Learning Summer School 2016

Rotation invariance



Credit: R. Fergus slides in Deep Learning Summer School 2016

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Is AlexNet rotation invariant?

- o Yes
- o No
- o In some cases

Is AlexNet rotation invariant?

- o Yes
- \circ No
- o In some cases

Rotation invariance



Credit: R. Fergus slides in Deep Learning Summer School 2016

Understanding convnets





How large filters?

- Traditionally, medium sized filters (smaller than 11×11)
- Modern architectures prefer small filter sizes (e.g. 3×3)





 \mathcal{VS} .



(Layer l) * (Layer l + 1)

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How large filters?

- Traditionally, medium sized filters (smaller than 11×11)
- Modern architectures prefer small filter sizes (e.g. 3×3)
- We lose frequency resolution
- Fewer parameters to train



 \mathcal{VS} .



(Layer l) * (Layer l + 1)

How large filters?

- Traditionally, medium sized filters (smaller than 11×11)
- Modern architectures prefer small filter sizes (e.g. 3×3)
- We lose frequency resolution
- Fewer parameters to train
- Deeper networks of cascade filters
 Still, the same output dimensionalities

For stride 1 the first feature map has dimensionality $\frac{H-2d-1}{1} + 1 = H - 2d$











 $(d+1)^2$



(Layer l) * (Layer l + 1)

*

For stride 1 the first feature map has dimensionality H - d, the second image $\frac{H - d - d - 1}{1} + 1 = H - 2d$

Filter invariance and equivariance

- Filters learn how
 different variances
 affect appearance
- Different layers and different hierarchies focus on different transformations
- For different objects
 filters reproduce
 different behaviors



Aubry et al., Understanding deep features with computer-generated imagery, 2015]

Figure 3: PCA embeddings for 2D position on AlexNet.

Filter invariance and equivariance



Figure 2: **Best viewed in the electronic version.** PCA embeddings (dims. 1,2) of AlexNet features for "chairs" (first row) and "cars" (second row). Column 1 – Direct embedding of the rendered images without viewpoint-style separation. Columns 2,3 – Embeddings associated with style (for all rotations) and rotation (for all styles). Column 4 – Rotation embedding for fc6, which is qualitatively different than pool5. Colors correspond to orientation and can be interpreted via the example images in columns 3,4. Similar results for other categories and PCA dimensions are available in the supplementary material.

Interesting questions

- What do the image activations in different layers look like?
- What types of images create the strongest activations?
- What are the activations for the class "ostrich"?
- Do the activations occur in meaningful positions?

- Convolution activations == feature maps
- A deep network has several hierarchical layers
 - hence several hierarchical feature maps going from less to more abstract



What excites feature maps?

• "Given a random feature map what are the top 9 activations?"



What excites feature maps?

Similar activations from lower level visual patterns



What excites feature maps? [Zeiler2014]



Visual patterns become more and more intricate and specific (greater invariance)



Feature evolution over training

- Given a neuron (outputs a single feature map)
 - Strongest activation during training for epochs 1, 2, 5, 10, 20, 30, 40, 64



But does a Convnet really learn the object?



What is a "Convnet dog", however? [Simonyan2014]

bell pepper

lemon

husky

Transfer learning

- \circ Assume two datasets, T and S
- \circ Dataset S is
 - fully annotated, plenty of images
 - \circ We can build a model $h_{\mathcal{S}}$
- \circ Dataset T is
 - Not as much annotated, or much fewer images
 - $^{\circ}$ The annotations of T do not need to overlap with S
- \circ We can use the model h_S to learn a better h_T
- This is called transfer learning

My dataset: 1,000

Why use Transfer Learning?

- A CNN can have millions of parameters
- But our datasets are not always as large
- Could we still train a CNN without overfitting problems?
Convnets are good in transfer learning

- Even if our dataset T is not large, we can train a CNN for it
- \circ Pre-train a network on the dataset S
- Then, there are two solutions
 - Fine-tuning
 - CNN as feature extractor

Solution I: Fine-tune h_T using h_S as initialization

- Assume the parameters of *S* are already a good start near our final local optimum
- Use them as the initial parameters for our new CNN for the target dataset

$$w_{T, t=0}^{l} = w_{S, t=\infty}^{l}$$
 for layers $l = 1, 2, ...$

- \circ Use when the target dataset T is relatively big
 - $^{\rm o}$ E.g. for Imagenet S with approximately 1 million images a dataset T with more than a few thousand images should be ok
- What layers to initialize and how?

Initializing h_T with h_S

- Classifier layer to loss
 - The loss layer essentially is the "classifier"
 - \circ Same labels ightarrow keep the weights from $h_{\mathcal{S}}$
 - $^{\circ}$ Different labels ightarrow delete the layer and start over
 - When too few data, fine-tune only this layer
- Fully connected layers
 - Very important for fine-tuning
 - Sometimes you need to completely delete the last before the classification layer if datasets are very different
 - Capture more semantic, "specific" information
 - Always try first when fine-tuning
 - If you have more data, fine-tune also these layers



Initializing h_T with h_S



- Mid-level spatial features (face, wheel detectors ...)
- Can be different from dataset to dataset
- Capture more generic information
- Fine-tuning pays off
- Fine-tune if dataset is big enough
- Lower convolutional layers (conv1, conv2)
 - They capture low level information
 - This information does not change usually
 - Probably, no need to fine-tune but no harm trying



How to fine-tune?

- \circ For layers initialized from h_S use a mild learning rate
 - Remember: your network is already close to a near optimum
 - If too aggressive, learning might diverge
 - A learning rate of 0.001 is a good starting choice (assuming 0.01 was the original learning rate)
- For completely new layers (e.g. loss) use aggressive learning rate
 - If too small, the training will converge very slowly
 - Remember: the rest of the network is near a solution, this layer is very far from one
 - A learning rate of 0.01 is a good starting choice
- If datasets are very similar, fine-tune only fully connected layers
- If datasets are different and you have enough data, fine-tune all layers



Solution II: Use h_s as a feature extractor for h_T

- Essentially similar to a case of solution I
 - but train only the loss layer
- Essentially use the network as a pretrained feature extractor
- \circ Use when the target dataset T is small
 - Any fine-tuning of layer might cause overfitting
 - Or when we don't have the resources to train a deep net
 - Or when we don't care for the best possible accuracy

Which layer?

Table 6. Analysis of the discriminative information contained in each layer of feature maps within our ImageNet-pretrained convnet. We train either a linear SVM or softmax on features from different layers (as indicated in brackets) from the convnet. Higher layers generally produce more discriminative features.

	Cal-101	Cal-256	
	(30/class)	(60/class)	L
SVM (1)	44.8 ± 0.7	24.6 ± 0.4	r
SVM(2)	66.2 ± 0.5	39.6 ± 0.3	← e
SVM (3)	72.3 ± 0.4	46.0 ± 0.3	C
SVM(4)	76.6 ± 0.4	51.3 ± 0.1	
SVM (5)	86.2 ± 0.8	65.6 ± 0.3	
SVM (7)	85.5 ± 0.4	71.7 ± 0.2	
Softmax (5)	82.9 ± 0.4	65.7 ± 0.5	
Softmax (7)	85.4 ± 0.4	72.6 ± 0.1	

Lower layer features capture more basic information (texture, etc). Good for image-to-image comparisons, image retrieval

Visualizing and Understanding Convolutional Networks, Zeiler and Fergus, ECCV 2014

Summary

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- Shared filters through local connectivity
- o Convolutions
- Convolutional Neural Networks
- Alexnet case study
- Visualizing ConvNets
- o Transfer learning

Reading material

o Chapter 9